

* Like terms:

- 1) The same variable
- 2) The same power.

$$* 5x, 3x, 7x, \frac{1}{2}x, -5\frac{1}{2}x$$

$$* 7xy, 2xy, \frac{3}{2}xy, -\frac{5}{4}xy$$

$$* 7x, 9x^2, 7y, -3z \quad \text{Not like}$$

Terms, Coefficient, variable, expression.

$$5x + 3y + 7$$

1) Polynomial.

2) $5, 3 \rightarrow$ Coefficient

3) $x, y \rightarrow$ variables.

4) $5x, 3y \rightarrow$ algebraic terms.

5) $7 \rightarrow$ free term.

6) $5x + 3y + 7 \rightarrow$ expression.

* Polynomial:

* Positive, Integer Power.

$$* 5x + 3y \quad \text{Polynomial}$$

$$* 7x^2 + 5x + 9 \quad \text{Polynomial}$$

$$* 7y + 4\sqrt{y} \quad \text{Not Polynomial.}$$

$$* \frac{5}{x} + 7 \rightarrow 5x^{-1} + 7 \quad \text{Not Polynomial.}$$

monomial \rightarrow one term $\rightarrow 7x, 5x, 3y,$

binomial \rightarrow Two terms $\rightarrow 7x + y, 5x - 4y$

Trinomial \rightarrow Three terms $\rightarrow 5x + 7y - 3$

Polynomial \rightarrow at least one term.

Adding & subtract:

$$5x + 3x = 8x$$

$$7x^2 - 2x^2 = 5x^2$$

$$4xy + 7xy = 11xy$$

$$5x + 3y = 5x + 3y$$

Multiply:

$$3x(x+5) = 3x^2 + 15x$$

$$-2x^2(3x+4) = -6x^3 - 8x^2$$

$$5xy(2x+3y-7) =$$

$$10x^2y + 15xy^2 - 35xy$$

$$(x+3)(2x-5) = 2x^2 - 5x + 6x - 15$$
$$= 2x^2 + x - 15$$

$$(5x-4)(3x+7) = 15x^2 + 35x - 12x - 28$$
$$= 15x^2 + 23x - 28$$

Note:

$$x^m \cdot x^n = x^{m+n}$$

$$x^m \div x^n = x^{m-n}$$

$$(x+3)(2x-5) = 2x^2 - 5x + 6x - 15$$

outer: $x \cdot (-5)$
inner: $3 \cdot 2x$

$$2x^2 + x - 15$$

First

Middle

Last

First = First \times First

Middle = Inner + outer

/ Last = Last \times Last

$$(a x + 3)(5 x - 7) = 20 x^2 + c x - 21$$

Find c ?

$$5a = 20 \rightarrow a = 4$$

$$c = 15 - 7a$$

$$15 - 7(4) = 15 - 28 = -13$$

$$\underline{5a} x^2 - 7a x + 15 x - 21 = \underline{20} x^2 + \underline{c} x - 21$$

$$5a = 20 \rightarrow a = 4$$

$$c = -7a + 15$$

$$= -7(4) + 15 = -13 \checkmark$$

* Expand:

$$(x + y)^2 = (\text{first})^2 + 2 \times \text{first} \times \text{Last} + (\text{last})^2$$

$$= x^2 + 2xy + y^2$$

$$(x + 5)^2 = x^2 + 2(x)(5) + 25$$

$$x^2 + 10x + 25$$

$$(2x - 7)^2 = 4x^2 - 2(2x)(7) + 49$$

$$4x^2 - 28x + 49$$

$$(x+y)(x-y) = (\text{First})^2 - (\text{Second})^2 \\ = x^2 - y^2$$

$$(x+5)(x-5) = x^2 - 25$$

$$(2x+3)(2x-3) = 4x^2 - 9$$